

Week 2 Lecture 1

Overview: Medical Signal Processing

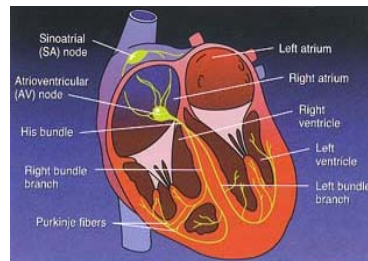
Why Medical Signal Processing?

Purposes:

- - Raw medical signals: Difficult to diagnosis
- - After transform, easier to find features
- - In many times, we need to use Machine Learning to further find “patient symptoms” from those features. This is called “Signal Learning”.
- - Sometimes we compress signals to save storage overhead.
- - Many times we need to remove noise from signals.
- - Use filters to remove high or low frequency components.
- - Many other signal processing purposes ...

Example: ECG signal analysis

- How do we know a patient has heart disease?
- Note: a cardiac doctor is not present – Thus we can only use computer to automatically recognize heart disease
- Today people use ECG sensor to collect heart beat signals
- Given an ECG sensor signal, how do we know if it is normal or not?



From a textbook
on cardiology

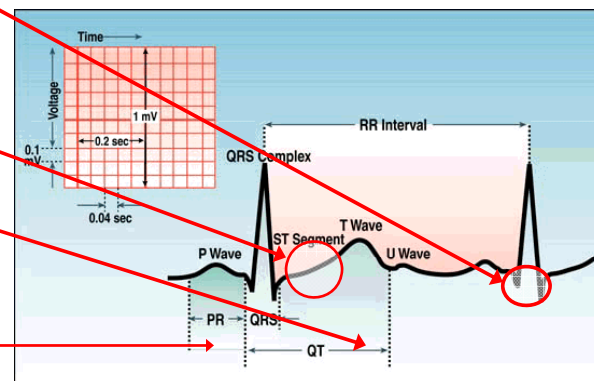
Clinically Relevant Parameters

- QRS duration
Bundle branch block
depolarization

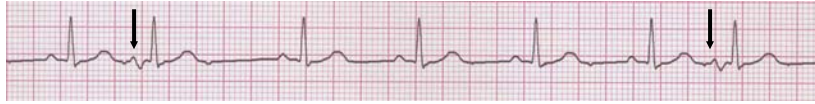
- ST segment
ischemia

- QT interval
ventricular fibrillation

- PR interval SA
→ ventricles



Rhythm example



- Rate? 70 bpm
 - Regularity? occasionally irreg.
 - P waves? 2/7 different contour
 - PR interval? 0.14 s (except 2/7)
 - QRS duration? 0.08 s
- Interpretation? *NSR with Premature Atrial Contractions*

Classification of ECG signals

E. Classification

- ① Linear discriminant analysis (LDA)

$$y = \alpha S + \varepsilon = \alpha_0 + \sum_{i=1}^n \alpha_i S_i + \varepsilon$$

- ② Quadratic discriminant analysis (QDA)

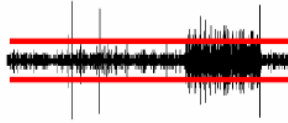
$$y = \alpha S + S^T \beta S + \varepsilon = \alpha_0 + \sum_{i=1}^n \alpha_i S_i + \sum_{i=1}^n \sum_{j=1}^n \beta_{ij} S_i S_j + \varepsilon$$

- ③ K nearest neighbor (KNN) rule

The present paper uses the Euclidean metric to measure “closeness” in the KNN classification model

Denoising

Threshold:



Stein's Unbiased Risk Estimate (SURE).

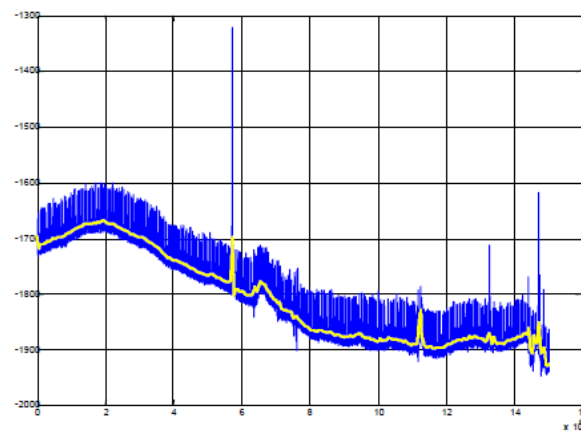
Donoho: $\lambda = \sigma \sqrt{2 \log(n)}$ n: Sample size
 σ : noise scale

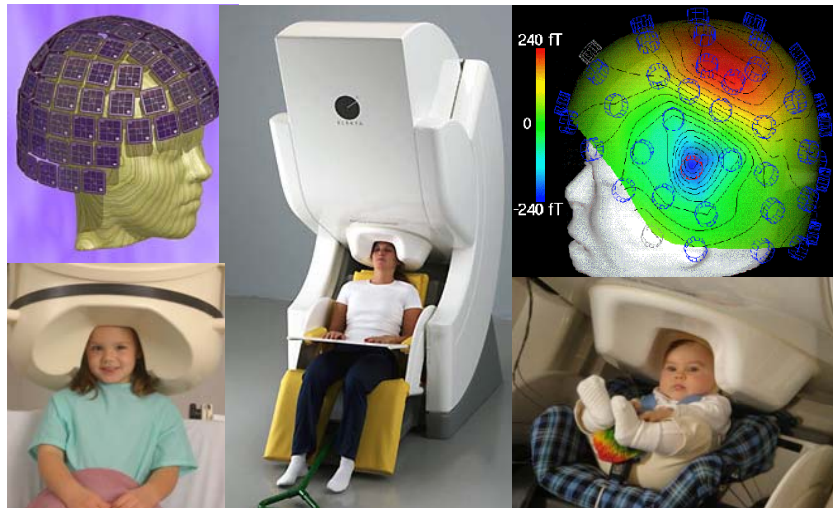
Minimax

Adaptive: based on singular or smooth regions
 (in practice, heuristic indep. of sample size)

Long-Term ECG Evolution

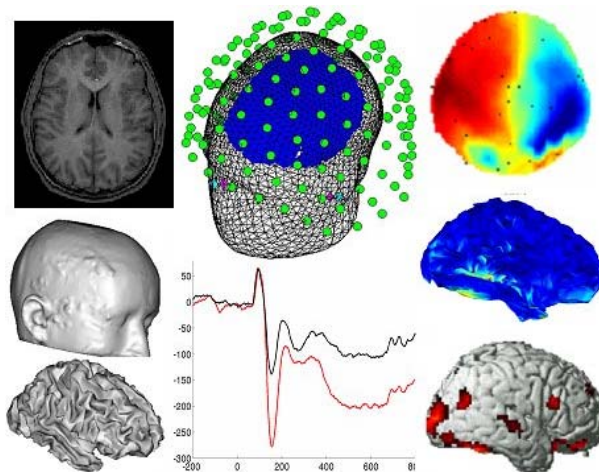
- Application: Electrocardiogram baseline wandering reduction





Magnetoencephalography (googled images)

Multimodal Imaging



- Combining MEG data with fMRI results in a hybrid image which has both good temporal and spatial resolution.

EEG

The diagram illustrates the EEG process. On the left, a cross-section of the brain shows the cerebral cortex with a layer of pyramidal cells. A small electrode is shown on the surface. In the center, a 3D model of a human head is shown with a grid of electrodes on the scalp. On the right, a blue EEG waveform is displayed. Below the diagram, two bullet points describe EEG as a tool for evaluating brain state and offering high resolution for characterizing electrical activity.

- Tool for evaluating the physiological state of the brain
- Offers excellent spatial and temporal resolution to characterize rapidly changing electrical activity of brain activation

MEDICAL TECHNOLOGY

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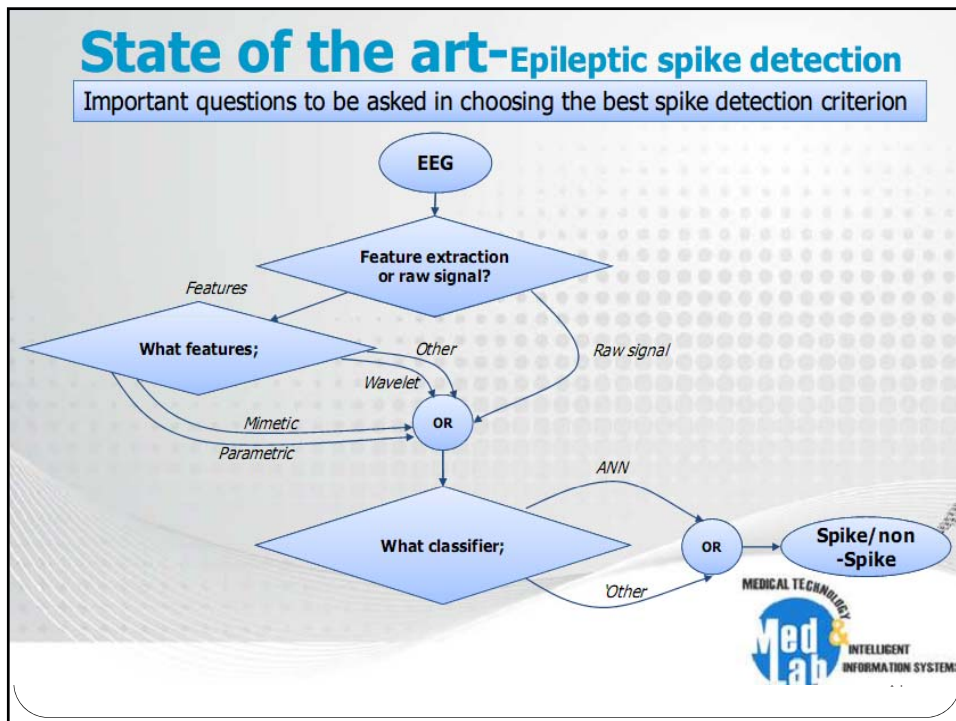
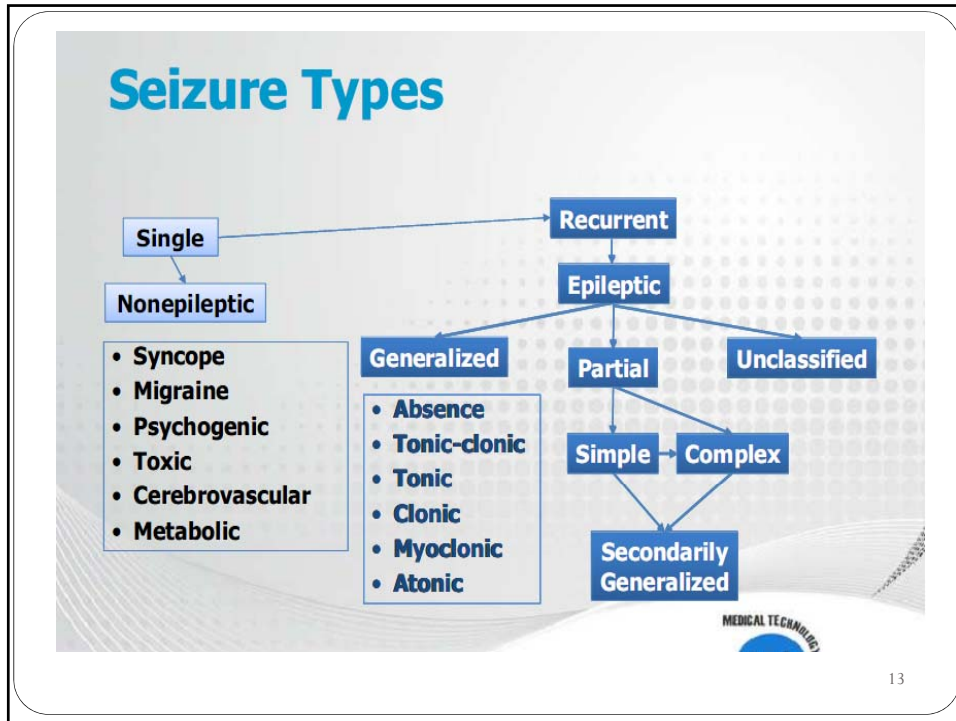
Epilepsy & EEG

The flowchart classifies epilepsy based on EEG signal abnormalities. 'Epilepsy' leads to 'Abnormal activity in EEG signal', which is divided into 'Inter-ictal' and 'Ictal'. 'Inter-ictal' is further categorized into 'Focal', 'Generalized', and 'Multi-local'. Below the flowchart, an EEG trace shows a transition from a normal signal to a 'Spike + Wave complex' at a point marked 'Onset'.

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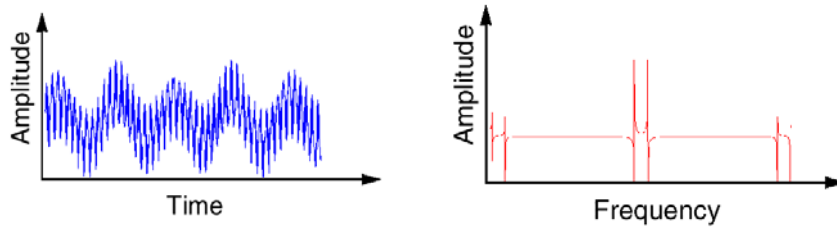
    graph TD
      Epilepsy([Epilepsy]) --> Abnormal[Abnormal activity in EEG signal]
      Abnormal --> Inter-ictal[Inter-ictal]
      Abnormal --> Ictal[Ictal]
      Inter-ictal --> Focal[Focal]
      Inter-ictal --> Generalized[Generalized]
      Inter-ictal --> Multi-local[Multi-local]
  
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Tool example: Fourier Analysis

- Breaks down a signal into **constituent sinusoids** of different frequencies



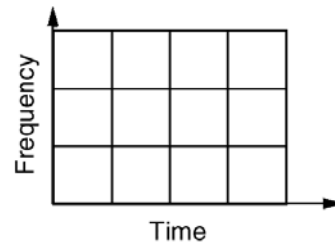
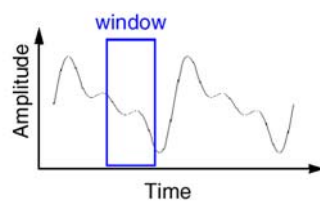
In other words: Transform the view of the signal from time-base to frequency-base.

Can we improve Fourier tool?

- By using Fourier Transform , we loose the time information : **WHEN** did a particular event take place ?
- FT can not locate drift, trends, abrupt changes, beginning and ends of events, etc.
- Calculating use complex numbers.

Short Time Fourier Analysis

- In order to analyze small section of a signal, Denis Gabor (1946), developed a technique, based on the FT and using windowing: STFT



What is Wavelet Analysis ?

- And...what is a wavelet...?

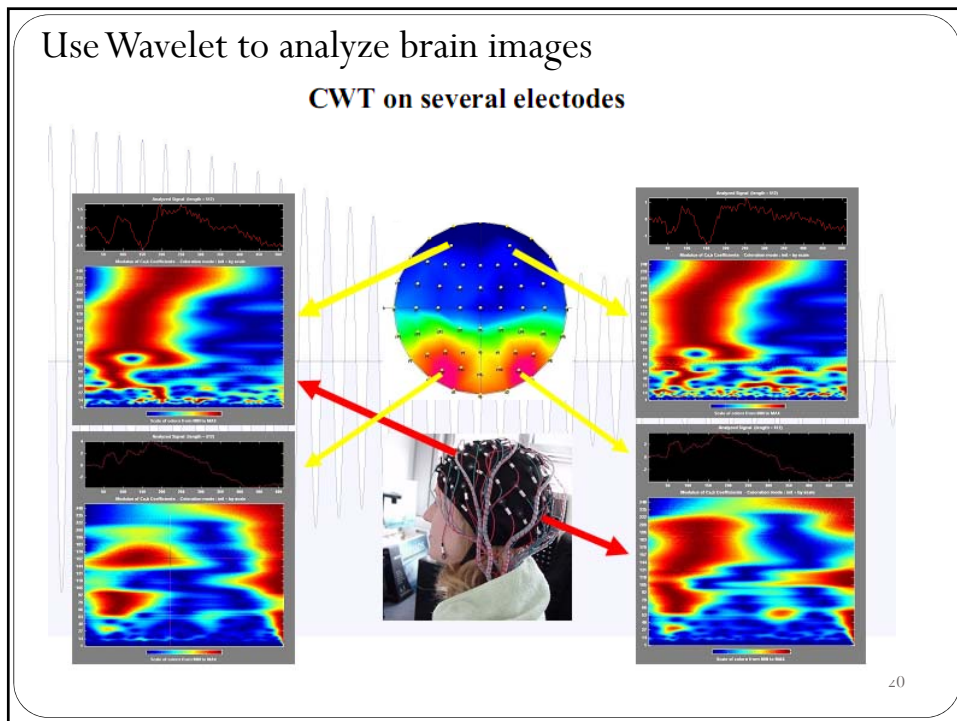
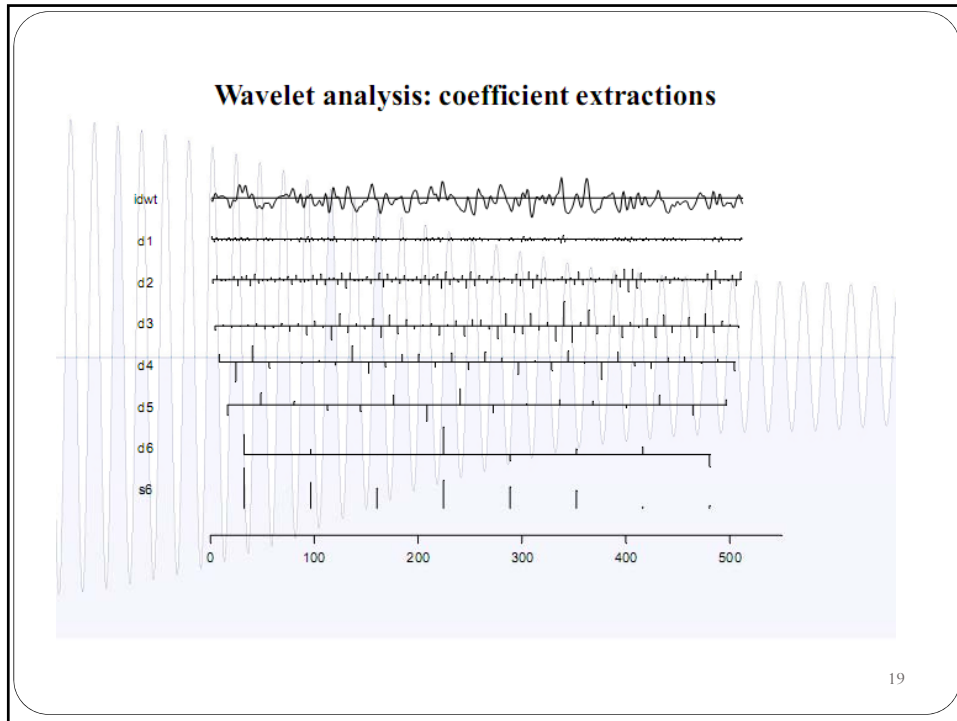


Sine Wave



Wavelet (db10)

- A wavelet is a waveform of effectively limited duration that has an average value of zero.



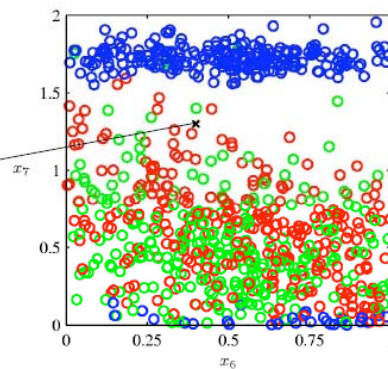
Machine Learning – A promising signal analysis tool

- Types of Problems Solved using ML
 1. Classification (class labels)
 - OCR, Handwritten digit recognition
 2. Regression (continuous values)
 - Ranking web pages using human or click data
 3. Clustering
 - No-label data classification
 4. Modeling - Inferring a Probability
 - seek probability distribution parameters

Classification example

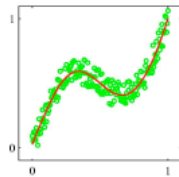
- Three classes (Stratified, Annular, Homogeneous)
- Two variables shown
- 100 points

Which class should x belong to?



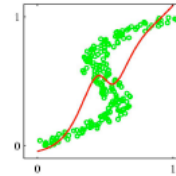
Regression problem

Forward problem
data set



Red curve is result of fitting a two-layer neural network by minimizing sum-of-squared error

Corresponding inverse problem by reversing x and t



Very poor fit to data:
GMMs used here

Clustering problem

- Old Faithful (Hydrothermal Geyser in Yellowstone)
 - 272 observations
 - Duration (mins, horiz axis) vs Time to next eruption (vertical axis)
 - Simple Gaussian unable to capture structure
 - Linear superposition of two Gaussians is better

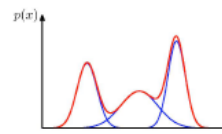
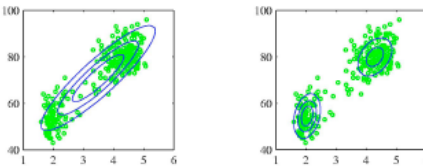


- Gaussian has limitations in modeling real data sets
- Gaussian Mixture Models give very complex densities

$$p(\mathbf{x}) = \sum_{k=1}^K \pi_k N(\mathbf{x} | \mu_k, \Sigma_k)$$

π_k are mixing coefficients that sum to one

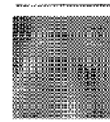
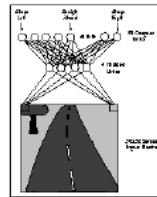
- One –dimension
 - Three Gaussians in blue
 - Sum in red



Example Successful Application of Machine Learning

- Learning to drive an autonomous vehicle
 - Train computer-controlled vehicles to steer correctly
 - Drive at 70 mph for 90 miles on public highways
 - Associate steering commands with image sequences

ALVINN [Pomerleau] drives 70 mph on highways



The ML Approach

